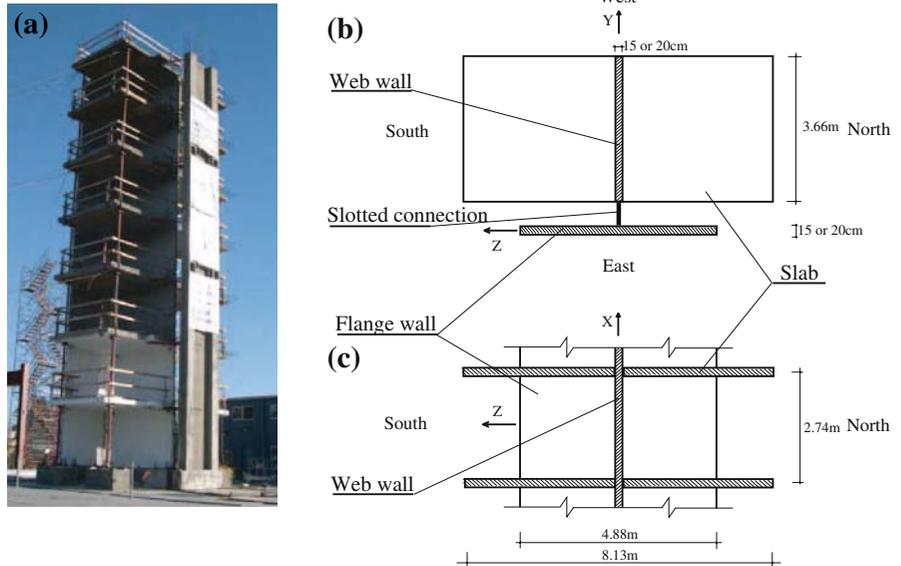




Fig. 1 a North West view of the test structure and geometrical data of the test structure [1]; b plan view, c elevation view



The aim of the study presented hereafter is to reproduce numerically the non linear behaviour of the full-scale vertical slice of the 7-story reinforced concrete walls building. Only the direction Y of loading is considered (parallel to the web wall). Four input motions at different intensities denoted EQ1, EQ2, EQ3 and EQ4 have been used with increasing maximum acceleration going from 0.15 to 0.85 g. Simulations are performed with FedeeasLab, a finite element Matlab toolbox developed by Pr. F. Filippou and his co-workers in UC Berkeley [9]. The building is modelled using Timoshenko multi beam elements [7, 9]. Constitutive material laws are based on damage mechanics to describe cracking of concrete and on plasticity for steel [2, 10]. The Timoshenko multi beam element and the damage mechanic law have been introduced into FedeeasLab by the 3S-R group.

In the first part of the paper, comparisons with the experimental response are “blind”, meaning that the experimental results were not known in advance. It is shown that the proposed modelling strategy describes accurately the global behaviour of the structure and qualitatively the distribution of damage at the base of the specimen. In the second part of the paper a comparison with the experimental results helps to identify the deficiencies of the original numerical model and to propose remedies to improve its performance.

We present hereafter in detail the experimental loading sequences, the mesh, the material parameters calculated numerically.

## 2 Input accelerations and spectra

Four input motions (denoted EQ1–EQ4) have been used for the experiments with increasing maximum acceleration going from 0.15 to 0.85 g. The first two records EQ1 and EQ2 come from the longitudinal and transverse components of the 1971 San Fernando earthquake, EQ3 comes from the longitudinal component of the 1994 Northridge earthquake and EQ4 corresponds to the 1994 Northridge earthquake Sylmar record as reproduced by the NEES-UCSD shaking table (Fig. 2).

EQ1 and EQ2 are quite long and have a high bandwidth of accelerations. Their peak ground accelerations are respectively 0.15 and 0.26 g. EQ3 and EQ4 are very close in terms of frequency content and have a thin bandwidth of high accelerations. Their peak ground accelerations are respectively 0.33 g and 0.85 g. The frequency content of the EQ4 signal is rich around 3.22 Hz (0.31 s) which is not so close to the natural frequency of the experimental structure (measured equal to 1.82 Hz (0.55 s)) (Fig. 3). Nevertheless, EQ3 and EQ4 response spectra present another peak at 10 Hz

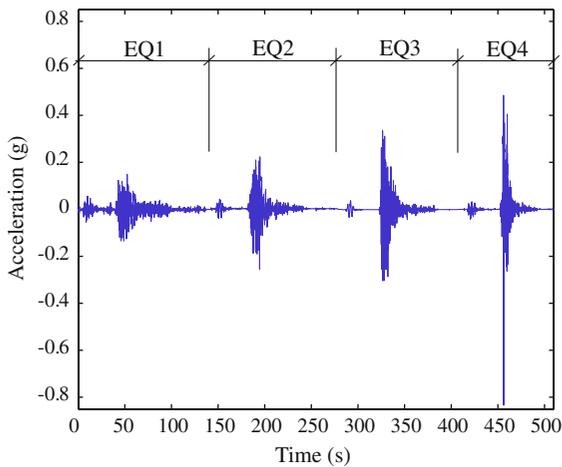


Fig. 2 Ground motions EQ1–EQ4.

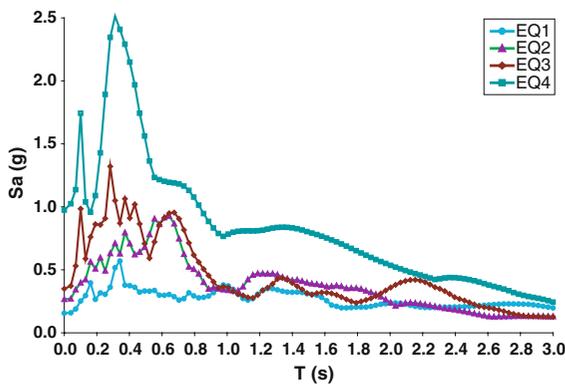


Fig. 3 Acceleration response spectra—5% damping [10]

### 3 Numerical model of the structure

#### 3.1 Spatial discretization

A good comprehension of the role of each structural element is important in order to choose the appropriate finite element mesh of the structure. The building is made of a web wall and a range wall connected by slotted connections. They constitute the main skeleton of the structure supporting the seven slabs. Reinforcement steel bars have a common density for this kind of structure in USA. More particularly, 8 bars of 8 mm diameter are used at both extremities of the web wall and 13 bars of 6 mm diameter distributed equally in its middle. Gravity columns permit to support the weight of the slabs and

they are positioned at their extremities. The dynamic excitation is applied only towards the Y direction (in the plane of the web wall, see Fig. 4). To avoid any 3D effects and particular any torsional mode, pre-cast segmental piers (PT columns) and bracing are used.

Because the dynamic excitation is unidirectional, the gravity columns, the pre-cast segmental pier and the bracing system are not taken into account into the numerical model presented hereafter. Fig. 4a gives a representation of the finite element discretization. The web wall and the range wall are decomposed into 19 multi-bay Timoshenko beam elements (four elements for levels 1 and 2, three elements for level 3 and two elements for levels 5–7). The slotted connections between the two walls are simulated using linear horizontal truss elements. Thus, only normal forces are transmitted. Four linear Bernoulli beam elements are used to reproduce the shaking table.

#### 3.2 Distribution of masses

Concentrated masses are considered at each floor taking into account the mass of the corresponding slab and the upper and lower part of the wall. They are presented in Tables 2 and Fig. 4a. The total mass of the structure is about  $M_{tot} = 182,000$  kg.

#### 3.3 Constitutive laws

Constitutive model for concrete under cyclic loading ought to take into account some observed phenomena such as decrease in material stiffness due to cracking, stiffness recovery which occurs at crack closure and inelastic strains concomitant to damage. To simulate this behaviour we use a damage model with two scalar variables, one in compression and one in tension [8]. Unilateral effect and stiffness recovery (damage deactivation) are also included. Inelastic strains are taken into account thanks to an isotropic tensor (Fig. 5). The total strain is given by:

$$\begin{cases} \epsilon = \epsilon^e + \epsilon^{in} \\ \epsilon^e = \frac{\langle \sigma \rangle_+}{E(1-D_1)} + \frac{\langle \sigma \rangle_-}{E(1-D_2)} + \frac{\nu}{E} (\sigma - Tr(\sigma)1) \\ \epsilon^{in} = \frac{\beta_1 D_1}{E(1-D_1)} \frac{\partial f(\sigma)}{\partial \sigma} + \frac{\beta_2 D_2}{E(1-D_2)} \end{cases} \quad (1)$$



Fig. 4 a Finite element mesh and concentrated masses and fibers in a given section

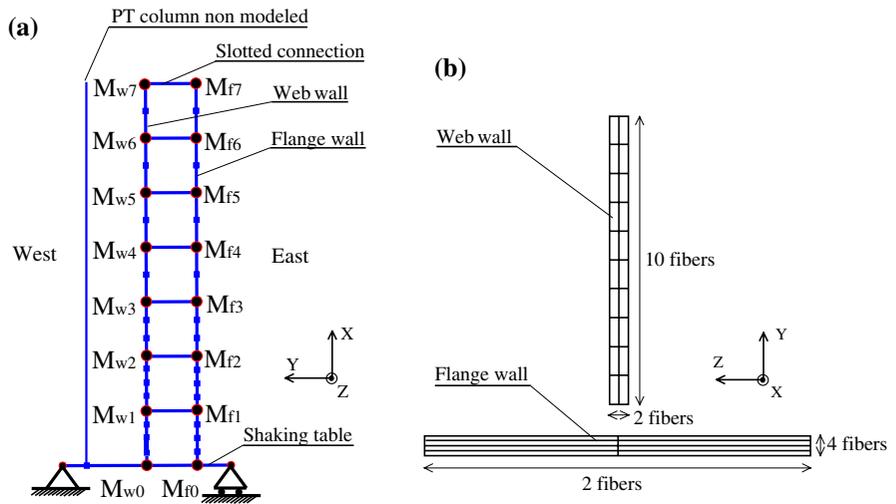


Table 1 Masses and rotational inertia for nodes in the web wall

Node	Masses $M_w$ (kg)	Rotational inertia $I_{wz}$ (kg m <sup>2</sup> )
w <sub>0</sub>	11,780	20,080
w <sub>1</sub>	18,470	23,100
w <sub>2</sub>	17,910	22,000
w <sub>3</sub>	17,910	22,000
w <sub>4</sub>	17,910	22,000
w <sub>5</sub>	17,910	22,000
w <sub>6</sub>	17,910	22,000
w <sub>7</sub>	16,200	22,000

Table 2 Masses and rotational inertia for nodes in the flange wall

Node	Masses $M_f$ (kg)	Rotational inertia $I_{fz}$ (kg m <sup>2</sup> )
f <sub>0</sub>	15,500	5,499
f <sub>1</sub>	5,376	3,582
f <sub>2</sub>	4,576	3,071
f <sub>3</sub>	4,576	3,071
f <sub>4</sub>	4,576	3,071
f <sub>5</sub>	4,576	3,071
f <sub>6</sub>	4,576	3,071
f <sub>7</sub>	2,126	1,535

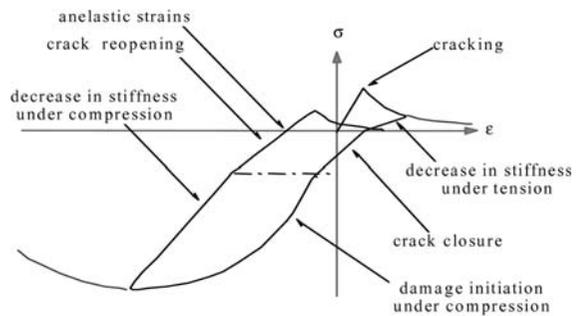


Fig. 5 Cyclic response of the La Borderie model

where

$$\begin{cases} Tr(\sigma) \in [0, +\infty) \rightarrow \frac{\partial f(\sigma)}{\partial \sigma} = 1 \\ Tr(\sigma) \in [-\sigma_f, 0] \rightarrow \frac{\partial f(\sigma)}{\partial \sigma} = \left(1 - \frac{Tr(\sigma)}{\sigma_f}\right) \\ Tr(\sigma) \in (-\infty, -\sigma_f] \rightarrow \frac{\partial f(\sigma)}{\partial \sigma} = 0 \end{cases} \quad (2)$$

with  $\epsilon^e$  the elastic strains,  $\epsilon^i$  the inelastic strains and  $\sigma$  the stress tensor.  $I$  denotes the unit tensor,  $Tr(\sigma) = \sigma_{ij}$ ,  $f$  is the crack closure function and  $\sigma_f$  the crack closure stress.  $\langle \cdot \rangle_+$  denotes the positive and  $\langle \cdot \rangle_-$  the negative part of the tensor.  $E_0$  is the initial Young's modulus and  $\nu_0$  the Poisson ratio.  $D_1$  and  $D_2$  are respectively the damage variables for tension and compression,  $\beta_1$  and  $\beta_2$  are material constants. Damage criteria are expressed as  $f_{d,i} = Y_i - Z_i$  ( $i = 1$



for tension or 2 for compression.  $Y_i$  is the associated force to the damage variable  $D_i$  and  $Z_i$  a threshold dependent on the hardening variables). The evolution laws for the damage variables are written as:

$$D_i = 1 - \frac{1}{1 + [A_i(Y_i - Y_{0i})]^{B_i}} \quad (3)$$

where  $Y_{0i}$  is the initial elastic threshold ( $Y_{0i} = Z_i(D_i = 0)$ ) and  $A_i$ ,  $B_i$  material constants. For the calculations presented hereafter the uniaxial version of the damage model is used (shear is considered linear). Figure 5 gives the stress–strain response of the model for an uniaxial tension-compression.

A modified version of the classical Menegotto-Pinto model [2, 10], with an isotropic hardening is used for steel.

The material data parameters of concrete and steel are fitted using the values provided in the contest rules. To simplify the problem only one type of concrete (concrete specimen number “c3f1” [12]) and steel are adopted. An ultimate compressive stress of  $f_c = 37.4$  MPa (=5.43 ksi) for a compressive strain of  $\varepsilon_{cu} = 0.00259$  is chosen and the Young modulus is taken equal to  $E = 24.46$  GPa (=3,549 ksi). In tension, the ultimate stress is  $f_t = 3$  MPa (=0.43 ksi) according to the empirical French rule  $f_t = 0.6 + 0.06 f_c$  [1]. The ultimate stress and yield stress for steel are taken equal to  $f_{su} = 710$  MPa (=103 ksi) and  $f_y = 450$  MPa (=65.3 ksi) respectively. The corresponding ultimate strain and yield strain are  $\varepsilon_{su} = 0.10$ , and  $\varepsilon_{sh} = 0.0060$ . These values lead to the material data parameters presented in Table

Table 3 Material data for the constitutive laws

Concrete parameters		Steel parameters	
$E$	24.46 GPa	$E$	200 GPa
$\nu$	0.2	$f_y$	450 MPa
$Y_{01}$	335 Pa	$f_{su}$	710 MPa
$Y_{02}$	0.05 MPa	$\varepsilon_{sh}$	0.0060
$A_1$	4,000 MPa <sup>-1</sup>	$\varepsilon_{su}$	0.10
$A_2$	4.01 MPa <sup>-1</sup>		
$B_1$	1.2		
$B_2$	1.335		
$\beta_1$	1 MPa		
$\beta_2$	-40 MPa		
$\sigma_f$	3.5 MPa		

### 3.4 Multi ber sections

The multi ber elements composing the web wall are divided into 20 concrete bres, whereas those of the angle wall are divided into eight concrete bres (Fig. 4b). The number and the position of the bres representing the longitudinal reinforcement steels are the same with those in the real section (see details of the sections in the contest rules [12]).

### 3.5 Stiffness of the shaking table

The shaking table is modelled using four linear elastic Bernoulli beam elements. The total length of the beams equals the length of the shaking table. Two of them are positioned below the structure having very high values of axial and bending stiffness. The bending stiffness of the two other beams is tuned according to the rotational stiffness provided by the official contest rules (Fig. 6).

### 3.6 Numerical strategy

The classical Newmark time integration scheme is used for the calculations assuming a constant variation of the acceleration ( $\alpha = \frac{1}{2}$  and  $\beta = \frac{1}{4}$ ). The secant Newton-Raphson strategy is chosen and the Rayleigh damping coefficients have been adjusted to ensure a value on 2% on the first and the fourth mode. P-delta effects are neglected and for computational reasons the four dynamic motions (EQ1–EQ4) have been launched independently (the structure is considered undamaged at the beginning of each loading).

## 4 Experimental versus “blind” prediction numerical results

### 4.1 Modal analysis

The modal analysis of the numerical model provides the natural frequencies and the modal shapes in Table 4 and Fig. 7. The first mode (bending) corresponds to a low frequency 1.74 Hz. This is to be compared with the only experimental mode measured after a white noise test (1.82 Hz).

Fig. 6 Tuning of the rotational stiffness of the shaking table

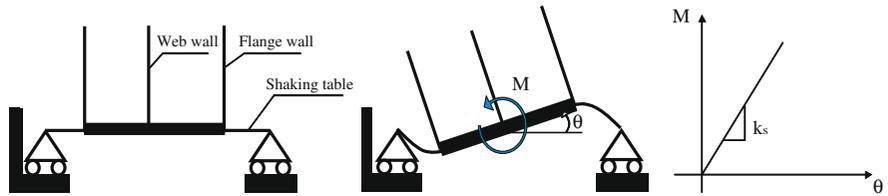


Table 4 Frequency and modes of the structure

Modes	Frequency (Hz)	Shape
1	1.74	Bending 0.25 T
2	7.94	Pumping(bending)
3	10.33	Bending 0.5 T

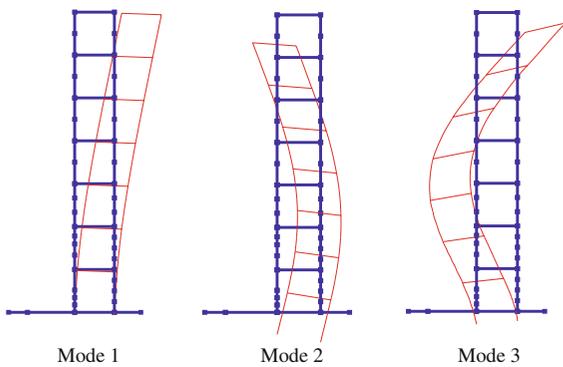


Fig. 7 Modal shapes

The second mode is actually a coupled bending-pumping mode. This deformed shape is due to eccentricity of the structure on the shaking table, which generated no-symmetrical displacements.

4.2 Non linear transient dynamic analysis

The maximum predicted and measured lateral displacements, floor accelerations, and inter-story drift ratios, for each level and for the four motions (EQ1–EQ4) are presented in Figs. 9 and 10.

The moment at the stage ( $M_i$ ) as well as the story shear force ( $V_i$ ) are evaluated based on the accelerations of each level (Eqs. 4, 5):

$$M_i = \sum_{k=i+1}^7 (M_{wi} + M_{fi}) \ddot{u}_{Yk} (X_k - X_i) \quad i \in [0; 6] \quad (4)$$

$$V_i = \sum_{k=i+1}^7 (M_{wi} + M_{fi}) \ddot{u}_{Yk} \quad i \in [0; 6] \quad (5)$$

where  $\ddot{u}_{Yk}$  is the horizontal acceleration according to Y axis of node k and  $X_k$  is the height (according to X axis) of node k.

The inter-story drift ratio for the story between the nodes i and i + 1 ( $ID_{i,i+1}$ ) is calculated according to Eq. 6:

$$ID_{i,i+1} = \frac{u_{Yi+1} - u_{Yi}}{X_{i+1} - X_i} \quad i \in [0; 6] \quad (6)$$

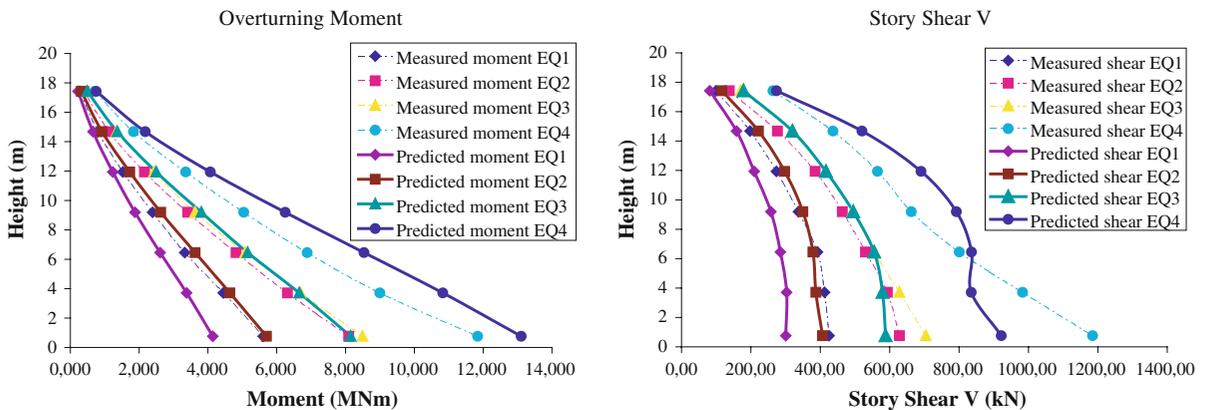


Fig. 8 Maximum overturning moments and story shear forces at different levels of the structure for the four sequences, comparisons between experimental (dotted lines) and “blind” prediction numerical results (continuous lines)



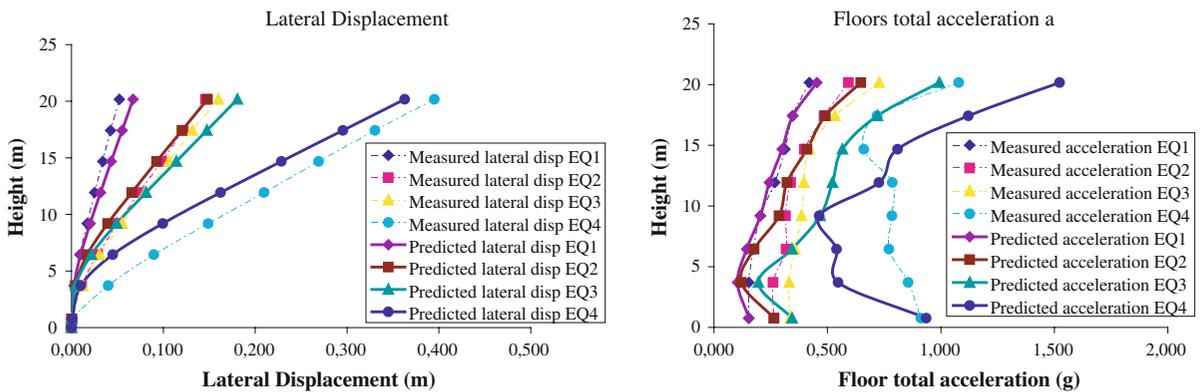


Fig. 9 Maximum lateral displacements and accelerations at different levels of the structure for the four sequences, comparisons between experimental (dotted lines) and “blind” prediction numerical results (continuous lines)

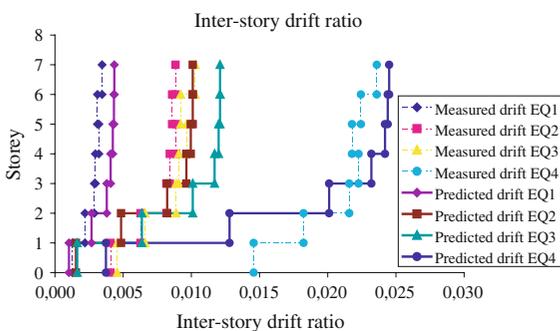


Fig. 10 Maximum interstory drift ratios in the structure for the four sequences, comparisons between experimental (dotted lines) and “blind” prediction numerical results (continuous lines)

where  $u_{yk}$  is the horizontal displacement according to  $Y$  axis of node  $k$  and  $X_k$  is the height (according to  $X$  axis) of node  $k$ .

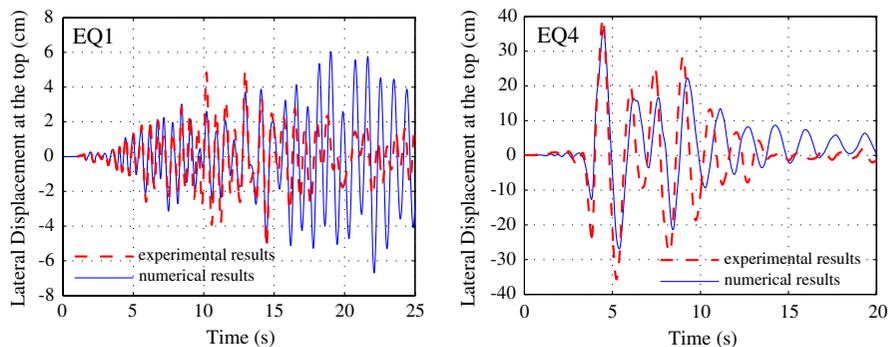
The “blind” predicted response is generally close to the experimental behaviour. Overturning moments and story shear forces are slightly underestimated for the EQ1 and EQ2 sequences and slightly

overestimated for sequence EQ4 (Fig. 10). Concerning the lateral displacements (Fig. 9), they are overestimated for sequence EQ1 and underestimated for sequence EQ4. In other words, the numerical structure is softer than the experimental one at the beginning of the tests, but is stiffer for the sequence EQ4. This difference comes certainly from the fact that the four dynamic motions have been launched independently in the numerical model. This is a point that needs to be improved in the future.

Accelerations at different levels of the structure for the different sequences are close to the experimental results (Fig. 9) except for the sequence EQ4 where maximum accelerations at the middle of the structure are lower. Interstory drift ratio given in Fig. 10 show clearly where the non-linearities are concentrated (high values of strains and damage).

The time histories of the calculated and experimental lateral displacements at the top of the structure for the EQ1 and the EQ4 sequences are presented in Fig. 11. For the EQ1 sequence, simulation satisfactorily predicts the behaviour until the first

Fig. 11 Lateral displacements at the top versus time for EQ1 and EQ4. Experimental (dashed lines) and “blind” prediction numerical results (continuous lines)



10 s. After that, the lateral displacement is overestimated. For the EQ4 sequence, the maximum displacement is correctly reproduced. Nevertheless, there is a shift between the curves at the loading.

5 Post-tests improvements of the numerical model

Two major improvements have been introduced to the original numerical model once the experimental results known. The first concerns the description of the continuity of the steel bars at the junction of levels 0 and 1 and the second a better “tuning” of the material and damping data. They are presented in detail hereafter.

5.1 Considering the continuity of steels at the junction of levels 0 and 1

Figure 12 shows the tension damage variable in the web wall section. This damage variable varies

normally between 0 (non damaged section) and 1.0 (completely damaged section). By iterating its value between 0.95 and 1.0, one can have an image of the distribution of the apparent cracks in the structure.

In the original numerical model, reinforcement bars were not considered at the junction between levels 0 and 1 (where the width of the section is reduced from 20 cm (8 inch) to 15 cm (6 inch)). This proved to be a mistake, leading to an unrealistic distribution of damage that was found to be concentrated all over the first two floors (Fig.12). By adding reinforcement bars at the junction, the link between the two levels is made stronger.

Figure 13 shows the tension damage variable in the web wall section considering the new more realistic distribution of reinforcement bars. Damage is now found to be concentrated at the base of the web wall (level 0) and only at the extremities of the wall at level 1. Comparison with the actual position of cracks at the end of the experiment shows that the model is now more capable to reproduce the trend observed experimentally.

Fig. 12 Initial numerical model: state of damage in concrete due to tension for the initial numerical model at levels 0 and 1 (EQ1)

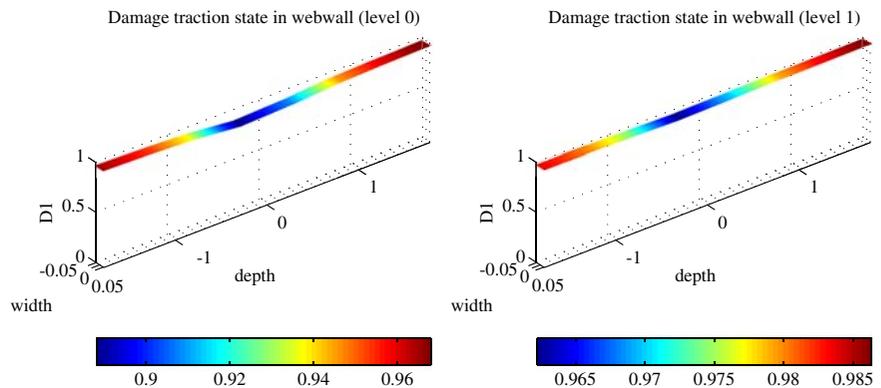
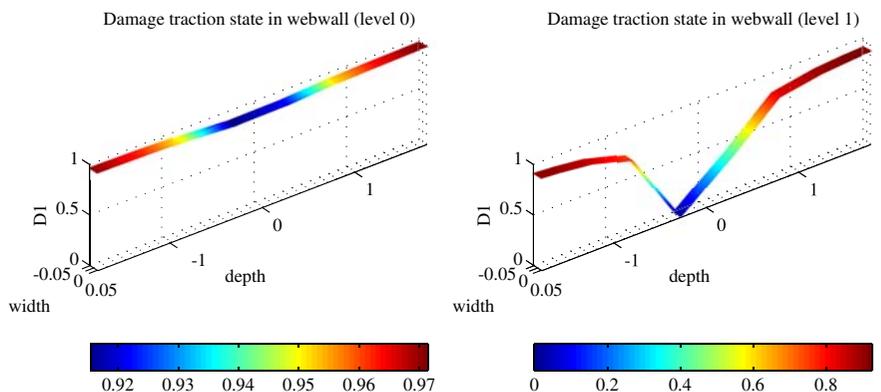


Fig. 13 Post-tests improvements—numerical model: state of damage in concrete due to tension for the modified numerical model at levels 0 and 1 considering continuity of steels (EQ1)



5.2 Considering new material and damping data

According to right picture of Fig.11, it is clear that the frequency of the numerical model is lower than the experimental one. In order to improve the numerical response the following material parameters have been changed: The concrete ultimate stress  $f_t$  is not known precisely. A new value is chosen equal to  $\sigma_t = 4$  MPa (=0.57 ksi). The steel yield stress  $f_y$  can be increased according to the values given in the contest rules. The new value is chosen equal to  $\sigma_y = 500$  MPa (=72.5 ksi). The last point concerns the coefficients of the Rayleigh damping. The new damping ratio applied to the first and the fourth modes is taken equal to 2.2%.

Comparison between the new numerical results for EQ4, the same trend is found for EQ1–EQ3 sequences in terms of the lateral displacements at the top of the structure is given in Fig.4 (continuity of steels is also taken into account). The numerical curves are now in phase with the experimental ones and the peaks are correctly reproduced.

5.3 Influence of the first mode on the behavior of the structure

The behaviour of the structure in terms of moments and displacements is primarily guided by the first mode. This can be identified by proceeding to the modal decomposition of the moments according to the Karhunen–Loève method [6]. Figure 15a and b show the static modal shape of the modal displacements (projection of the displacements on the modal space) and modal moments (projection of the moments on the modal space). It is obvious that the first mode contributes significantly to the moments developed in the structure and displacements. Although the results presented in Fig.5 are only

6 Conclusion and way forward

As demonstrated throughout this work, a modelling strategy based on Timoshenko multi beam

Fig. 14 Post-tests improvements: lateral displacements at the top versus time for EQ1 and EQ4. Experimental (dashed lines) and numerical results (continuous lines) considering new material and damping data and continuity of steels

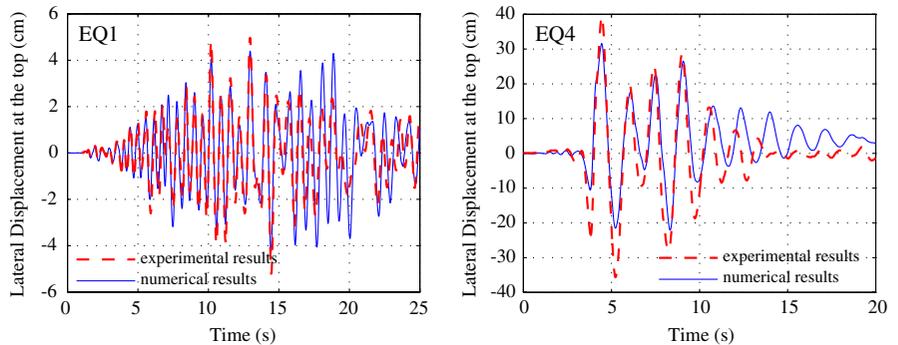
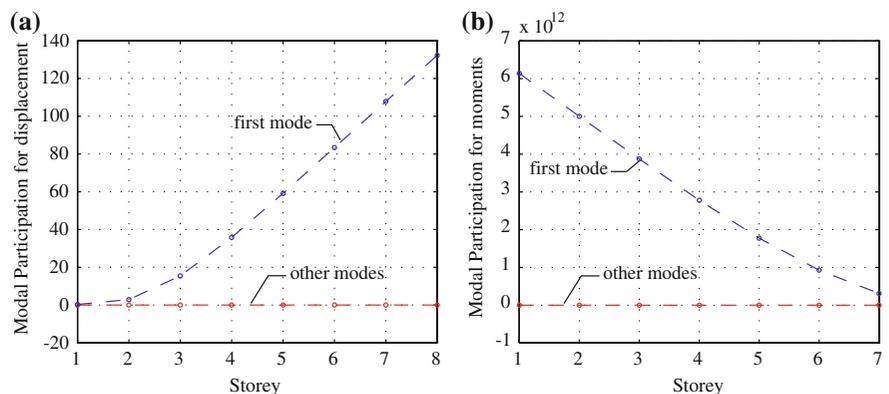


Fig. 15 Post-tests improvements—numerical model: static modal shape of the displacements (a) and moments (b)



elements and constitutive laws within the framework of damage mechanics for concrete and plasticity for steel is able to reproduce with good approximation the global response of the 7-story NEES building and qualitatively the distribution of damage (“blind” calculations). Moreover, this simplified approach helps to reduce computational costs (one loading sequence takes only a couple of hours with Matlab). Once the experimental results were available, improvements were obtained to the initial model by reproducing correctly the continuity of the reinforcement bars and by adjusting some material and damping parameters. We would like at this point to emphasize again the importance of reproducing accurately the actual length of the reinforcement bars in the finite element mesh. Otherwise, local results (i.e. damage variables) may be misleading. Finally, the application of the Karhunen-Löve method [6] is a very useful tool to gain insight into the behaviour of the structure. For the NEES specimen, it is shown that the behaviour is mainly guided by the first mode.

It appears now possible to use this kind of modelling strategy to investigate numerically the behaviour of a wider variety of configurations that is practically impossible to study experimentally. For example, the influence of Soil Structure Interaction (SSI) on the behaviour of the NEES structure for different types of soils is studied in Grange et al. [4]. It is done by introducing a recently developed macro-element [5] between the multi-ber Timoshenko beams modelling the structure and the shaking table. The first results show, as expected, a reduction of the internal forces and an increase of the displacements at the top of the structure but also, a shifting in the excitation of the modes. Such numerical tools are necessary for the practical engineer in order to reproduce satisfactorily the non-linear behaviour of a structure and the interaction with its boundary conditions.

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of Reinforced Concrete Walls” held in San Diego the 15th and 16th of December 2006.

## References

1. BAEL91 (2000) Règles techniques de conception et de calcul des ouvrages et constructions en béton armé suivant la méthode des états-limites. Eyrolles, Paris, France
2. Filippou FC, Popov EP, Bertero VV (1983) Effects of bond deterioration on hysteretic behaviour of reinforced concrete joints. Technical Report EERC-83/19. Earthquake Engineering Research Center, University of California, Berkeley
3. Filippou FC, Constandines M (2004) FedeeasLab getting started guide and simulations examples. Department of Civil and Environmental Engineering, UC Berkeley
4. Grange S, Kotronis P, Mazars J (2007) Extensive validation of the SSI macro element using experimental and numerical results. Deliverable [D8-2], European Contract LESSLOSS, Project No.: GOCE-CT-2003-505488, Risk Mitigation for Earthquakes and Landslides, Sixth Framework Programme. <http://hal.archives-ouvertes.fr/hal-00138210>
5. Grange S, Kotronis P, Mazars J (2008) A macro-element for a circular foundation to simulate 3D soil-structure interaction. *Int J Numer Anal Methods Geomech* 32(10): 1205–1227
6. Gutiérrez E, Zaldivar JM (2000) The application of Karhunen-Löve, or principal component analysis method, to study the non-linear seismic response of structures. *Earthq Eng Struct Dyn* 29:1261–1286
7. Kotronis P, Mazars J (2005) Simplified modelling strategies to simulate the dynamic behaviour of r/c walls. *J Earthq Eng* 9(2):285–306
8. La Borderie C (1991) *Plumes unilatérales dans un matériau endommageable: modélisation et application à l'analyse des structures en béton*. PhD thesis, Université Paris 6
9. Mazars J, Kotronis P, Ragueneau F, Casaux G (2006) Using multi-ber beams to account for shear and torsion. Applications to concrete structural elements. *Comput Methods Appl Mech Eng* 195(52):7264–7281
10. Menegotto M, Pinto P (1973) Method of analysis of cyclically loaded reinforced concrete plane frames including changes in geometry and non-elastic behaviour of elements under combined normal force and bending. In: IABSE Symposium on resistance and ultimate deformability of structures acted on by well-defined repeated loads, final report, Lisbon, p 328
11. NEES7story website (2006) NEES/UCSD seven-story building-slice earthquake blind prediction contest. <http://nees.ucsd.edu/7Story.html>
12. NEES7story report (2006) NEES/UCSD workshop and seminar on analytical modeling of reinforced concrete walls for earthquake resistance. (Report), UC San Diego, USA—California, December 15–16